

Cambridge O Level

CANDIDATE NAME		
CENTRE NUMBER		CANDIDATE NUMBER
ADDITIONAL MATHEMATICS 4037/23		
Paper 2		October/November 2021
		2 hours

You must answer on the question paper.

No additional materials are needed.

INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.

This document has 16 pages. Any blank pages are indicated.

 Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 80.
- The number of marks for each question or part question is shown in brackets [].

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Mathematical Formulae

1. ALGEBRA

Quadratic Equation

For the equation $ax^2 + bx + c = 0$,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Binomial Theorem

$$(a+b)^{n} = a^{n} + \binom{n}{1}a^{n-1}b + \binom{n}{2}a^{n-2}b^{2} + \dots + \binom{n}{r}a^{n-r}b^{r} + \dots + b^{n}$$

where *n* is a positive integer and $\binom{n}{r} = \frac{n!}{(n-r)!r!}$

Arithmetic series
$$u_n = a + (n-1)d$$

 $S_n = \frac{1}{2}n(a+l) = \frac{1}{2}n\{$

$$S_n = \frac{1}{2}n(a+l) = \frac{1}{2}n\{2a+(n-1)d\}$$

Geometric series

$$u_n = ar^{n-1}$$

$$S_n = \frac{a(1-r^n)}{1-r} \quad (r \neq 1)$$

$$S_{\infty} = \frac{a}{1-r} \quad (|r| < 1)$$

2. TRIGONOMETRY

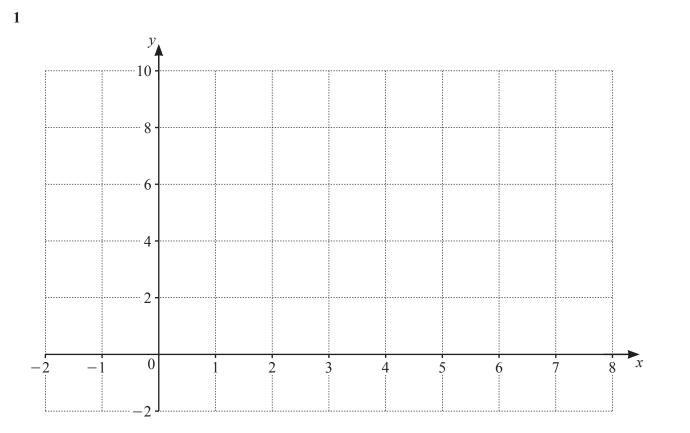
Identities

$$\sin^2 A + \cos^2 A = 1$$
$$\sec^2 A = 1 + \tan^2 A$$
$$\csc^2 A = 1 + \cot^2 A$$

Formulae for $\triangle ABC$

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$
$$a^{2} = b^{2} + c^{2} - 2bc \cos A$$
$$\Delta = \frac{1}{2}bc \sin A$$

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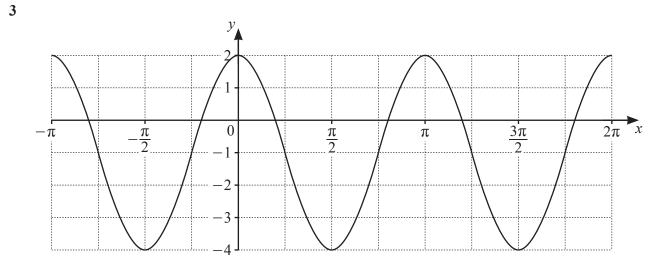
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(a) On the axes draw the graphs of y = |x-5| and y = 6 - |2x-7|. [4]

(b) Use your graphs to solve the inequality
$$|x-5| > 6 - |2x-7|$$
. [2]

2 Solve the following simultaneous equations. Give your answers in the form $a + b\sqrt{3}$, where a and b are rational.

$$\begin{aligned} x+y &= 3\\ 2x-\sqrt{3}y &= 5 \end{aligned}$$
[5]



(a) The curve has equation $y = a \cos bx + c$ where a, b and c are integers. Find the values of a, b and c. [3]

- (b) Another curve has equation $y = 2\sin 3x + 4$. Write down
 - (i) the amplitude,
 - (ii) the period in radians.

[1]

[1]

4 (a) Solve the equation $\log_6(2x-3) = \frac{1}{2}$. Give your answer in exact form. [2]

(b) Solve the equation $\ln 2u - \ln(u - 4) = 1$. Give your answer in exact form. [3]

(c) Solve the equation
$$\frac{3^{\nu}}{27^{2\nu-5}} = 9.$$
 [3]

5 (a) Show that
$$\frac{1}{\csc x - 1} + \frac{1}{\csc x + 1} = 2\tan x \sec x$$
.

(b) Hence solve the equation $\frac{1}{\csc x - 1} + \frac{1}{\csc x + 1} = 5 \csc x$ for $0^\circ < x < 360^\circ$. [4]

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[2]

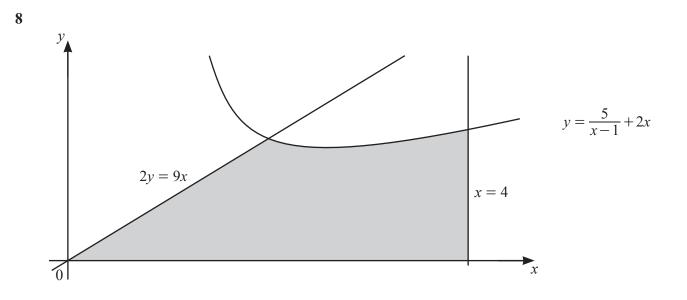
- 6 It is given that $x = 2 + \sec \theta$ and $y = 5 + \tan^2 \theta$.
 - (a) Express y in terms of x.

(b) Find
$$\frac{dy}{dx}$$
 in terms of x. [1]

(c) A curve has the equation found in **part (a)**. Find the equation of the tangent to the curve when $\theta = \frac{\pi}{3}$. [4]

- 7 The vector **p** has magnitude 39 and is in the direction -5i+12j. The vector **q** has magnitude 34 and is in the direction 15i-8j.
 - (a) Write both **p** and **q** in terms of **i** and **j**. [4]

(b) Find the magnitude of $\mathbf{p} + \mathbf{q}$ and the angle this vector makes with the positive x-axis. [4]



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The diagram shows part of the curve $y = \frac{5}{x-1} + 2x$, and the straight lines x = 4 and 2y = 9x. (a) Find the coordinates of the stationary point on the curve $y = \frac{5}{x-1} + 2x$. [5]

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- **9** An arithmetic progression has first term *a* and common difference *d*. The third term is 13 and the tenth term is 41.
 - (a) Find the value of a and of d.

[4]

(b) Find the number of terms required to give a sum of 2555.

[4]

(c) Given that S_n is the sum to *n* terms, show that $S_{2k} - S_k = 3k(1+2k)$. [4]

10 (a) It is given that $f(x) = 4x^3 - 4x^2 - 15x + 18$. Find the equation of the normal to the curve y = f(x) at the point where x = 1. [5]

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(b) DO NOT USE A CALCULATOR IN THIS PART OF THE QUESTION.

It is also given that x + a, where *a* is an integer, is a factor of f(x). Find *a* and hence solve the equation f(x) = 0. [6]

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